

Stumbling with optimal phase reset during gait can prevent a humanoid from falling

Masao Nakanishi · Taishin Nomura · Shunsuke Sato

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Abstract The human biped walking shows phase-dependent transient changes in gait trajectory in response to external brief force perturbations. Such responses, referred to as the stumbling reactions, are usually accompanied with phase reset of the walking rhythm. Our previous studies provided evidence, based on a human gait experiment and analyses of mathematical models of gait in the sagittal plane, that an appropriate amount of phase reset in response to a perturbation depended on the gait phase at the perturbation and could play an important role for preventing the walker from a fall, thus increasing gait stability. In this paper, we provide a further material that supports this evidence by a gait experiment on a biped humanoid. In the experiment, the impulsive force perturbations were applied using push-impacts by a pendulum-like hammer to the back of the robot during gait. The responses of the external perturbations were managed by resetting the gait phase with different delays or advancements. The results showed that appropriate amounts of phase resetting contributed to the avoidance of falling against the perturbation during the three-dimensional robot gait. A parallelism with human gait stumbling reactions was discussed.

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M. Nakanishi · T. Nomura (✉)
Division of Bioengineering,
Graduate School of Engineering Science, Osaka University,
1-3 Machikaneyama, Toyonaka, Osaka 560-8531, Japan
e-mail: taishin@bpe.es.osaka-u.ac.jp

S. Sato
Aino University, 4-5-4, Higashi-Ohda, Ibaraki,
Osaka 567-0012, Japan

1 Introduction

Human biped gait in its steady state possesses dynamic stability, implying that it may be modeled as a stable limit cycle solution of the neuro-musculo-skeletal system as a coupled nonlinear dynamical system (Taga 1995). Gait responses following single, usually short-lived, force perturbations during steady gait could be viewed as transient dynamics of the underlying system in which the system's state point asymptotes back to the limit cycle. Such responses are often referred to as the stumbling reactions in the field of neurophysiology (Forssberg 1979). The stumbling reactions include lowering and elevating strategies, one of which is chosen by the walking subject depending on the timing, i.e., the phase within the gait cycle at which a type of perturbation is applied (Schillings et al. 1999, 2000; Forner Cordero et al. 2003, 2004), in particular during stumbling over obstacles. The gait cycle duration may change during the reaction, but its steady-state value is reestablished after the transient, leading to the phase reset of the walking rhythm in the Winfree's sense (Winfree 1980; Kawato 1981). For a type of perturbation during human gait, we have demonstrated the amount of the phase reset as the function of the perturbation phase, i.e., phase resetting curve (Kobayashi et al. 2000). Moreover, we showed that the transient duration (settling time) was also phase dependent.

Physiological studies have long been providing evidences in animals and human that the basic walking rhythm is generated by a distributed neural network in the central nervous system (CNS), referred to as the central pattern generator (CPG) (e.g., Grillner 1981; Dimitrijevic et al. 1998), and it has been modeled as an autonomous nonlinear oscillator. Since there is

one-to-one correspondence between the CPG oscillations and the walking cycles during steady gait, the phase reset of the walking rhythm during the stumbling reaction is necessarily accompanied with the phase reset of the CPG by the same amount.¹ For a given perturbation, how much should the phase be reset? How long should it take in order to maintain dynamic stability against the perturbations during gait? How are they determined? Although it is intuitively evident that the stumbling reactions with the phase reset provide a basis of maintenance of postural stability during gait, necessary conditions that should be satisfied by the reactions are not trivial. Yamasaki et al. (2003a,b) partly answered the first question by using a mathematical model of biped human walking. Their model was defined on the sagittal plane with seven rigid links, and the ground reaction force was modeled by nonlinear hard springs and viscous elements. They showed, for almost every examined phase of the perturbation, that there exists a range of the optimal amounts of phase reset with appropriate transient durations. Their result was consistent with the experimental result shown by Kobayashi et al. (2000) during human gait. They considered two biped models: one included a mechanism of the optimal phase reset that could prevent the model from a fall in response to a given perturbation (closed-loop model), and the other did not (open-loop, master-slave model) in which the perturbation might lead to falling. Assuming both models span the identical phase space, examination of basin of attraction of each model's limit cycle clarified that the basin of the former model is wider than that of the latter. That is, a state point of the model without phase reset mechanism located outside the basin due to the perturbation could be inside the basin for the model with the appropriate phase reset.

In the present study, we applied the phase resetting mechanism that could increase gait stability to the humanoid gait, and tried to demonstrate experimentally that the stumbling reaction with optimal phase resets can prevent the walking humanoid from a fall. To this end, a humanoid robot was used in this study, and the use of the robot was motivated by the following reasons. (1) Unlike in the case of numerical simulation of biped gait, a real-world robot experiment does not require mathematical modeling of the ground reaction forces and frictions that are usually difficult to deal with. Thus, experimental results can be interpreted without

discussing effects of a degree of accuracy of the ground reaction force modeling. (2) The phase resetting mechanism itself merely deals with a modification of gait phase, and thus postural balancing in the mediolateral direction, which has not been taken into account in the sagittal modeling (Yamasaki et al. 2003a,b), is not explicitly considered, but the robot movements occur in the three-dimensional space. The robot experiment here in the real world showed that these issues were not dominant factors for the phase reset mechanism to maintain the gait against perturbations in the anteroposterior direction, and the theory developed for the simple gait model on the sagittal plane could be extended into the real-world gait.

Our experimental approach was straightforward, in which the robot movement in terms of its joint angles just followed a prescribed trajectory and no control mechanisms compensating the perturbation were used other than the phase resetting which involves modification of the prescribed trajectory in response to the perturbation for a certain period of transient time. In this way, we could have a concentrated look at the role played by the phase resetting to increase gait stability. Results confirmed in this study will be discussed with related studies performed during human gait.

2 Methods

2.1 Humanoid robot

A small biped humanoid robot (HOAP-1, Fujitsu, Japan) was used for the study. The height and weight of the robot are 48 cm and 6 kg, respectively. The total degrees of freedom (dof) of the robot are 20, including 6 dof for each leg and 4 dof for each arm. Every dof is actuated by a DC motor controlled locally by a microcomputer. The main control of the robot movement is made by a PC with RT-Linux (FMV-C600, CPU: Pentium4, 1.7 GHz). The microcomputer for each motor receives a desired joint angle every 1 ms from the PC and the high gain local servo mechanism with the microcomputer and the corresponding DC motor forces the joint angle of the robot to coincide with the desired joint angle. Let us denote a sequence of desired joint angles for all of 20 dof used for the current study as the *motion data*. A motion data, represented here in a matrix form just for convenience, included 20 columns corresponding to 20 dof and N rows. A motion data providing a joint angle trajectory of the robot for a time interval N ms from the beginning of the movement to the end was prescribed and fed into the PC controller. The robot includes a three-axial acceleration sensor and a

¹ If we simply assume that the CPG is a master oscillator of the mechanical body-limbs as a slave, the phase reset of the CPG results in that of the walking rhythm. Animal and human gait control systems, however, are not so simple. Nevertheless, such a simplification may help our understanding of gait control.

154 three-axial angular velocity sensor within the body to
 155 detect the motion of the center of the body mass. Each
 156 of 20 motors has an optical rotary encoder to detect
 157 the joint angle. Every joint angle shown below is rep-
 158 resented as a relative rotated angle between two adja-
 159 cent limbs in radian measured from the standard upright
 160 standing posture. In cases of the hip and knee, positive
 161 joint angles stand for flexion. For the ankle, negative
 162 angles for dorsiflexion. Each foot has force sensors at its
 163 four corners, and the total ground reaction force (GRF)
 164 only in the vertical direction of each foot was obtained
 165 as the summation of those, and represented as the ratio
 166 to the total weight of the robot (normalized GRF).

167 2.2 Control gait of the humanoid

168 In the experiment, basically, only one motion data was
 169 used, and all joints of the robot moved in accordance
 170 strictly with this motion data, even if the robot was per-
 171 turbed, unless the motion data provided to the robot was
 172 modified. This was possible because of the high gain
 173 local servo at every joint. The humanoid gait without
 174 any modification from the motion data was used as a
 175 reference, and referred to as the *control gait*, and the
 176 corresponding motion data as the *control motion data*.
 177 Perturbed gaits with some modifications from the con-
 178 trol gait will be defined below. The control gait spanned
 179 17,900 ms time interval. The control gait started with
 180 a quiet standing posture, and the robot made 12 steps,
 181 and then stopped. The middle part of the control gait
 182 (about 7,000 ms after the beginning of the gait until
 183 about 13,000 ms) could be considered as a steady walk-
 184 ing and its gait cycle (period) was about $T \simeq 2,600$ ms.
 185 The average walking velocity was 4.3 cm/s. Throughout
 186 the study, the robot walking was performed on a pine
 187 wooden plate with 2 cm thickness by which the control
 188 gait was the most stable (see Fig. 1).

189 2.3 Perturbation and perturbed gait

190 Figure 1 shows the experimental setup used for the study.
 191 The robot walking was performed on the wooden plate
 192 located in the steel-pipe-cage. A hard elastic rubber-
 193 hammer with 0.25 kg weight was attached to one edge
 194 of an aluminum stick with 62 cm length. The other edge
 195 was attached to the top of the cage to behave as a pen-
 196 dulum. The rotational joint of the pendulum was con-
 197 sidered as a frictionless hinge. A light steel plate was
 198 attached on one face of the hammer, and the pendulum
 199 with the hammer was fixed at one end of the cage by
 200 an electric magnet, where the pendulum was elevated 30°
 201 from the vertical. At the beginning of the robot gait, the
 202 electric magnet was powered. During the robot walking,

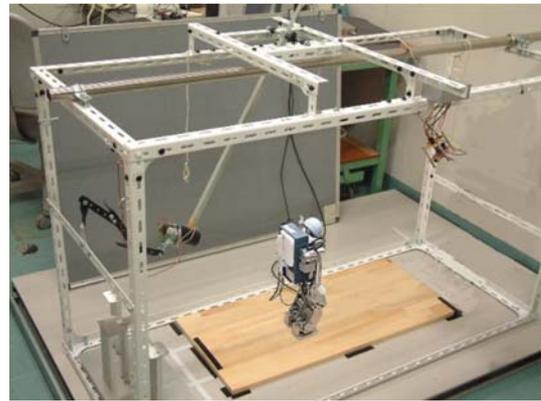


Fig. 1 Experimental setup. The robot (HOAP-1) walking was performed on the wooden plate located in the steel-pipe-cage. A hard elastic rubber-hammer with 0.25 kg weight was attached at one edge of an aluminum stick with 62 cm length, and the other edge was attached at the top of the cage to behave as a pendulum. A light steel plate was attached on one face of the hammer, and the pendulum with the hammer was fixed at one end of the cage by an electric magnet, where the pendulum was elevated 30° from the bottom. At the beginning of the robot gait, the electric magnet was powered. During robot walking, the electric power was switched off to release the hammer and then to apply a single impulsive force perturbation to the back of the robot body (trunk). See text

203 the electric power was switched off to release the ham-
 204 mer and then to apply a single impulsive force perturba-
 205 tion to the back of the robot body (trunk). The back of
 206 the robot body was covered by a styrol plate with 1 cm
 207 thickness to avoid mechanical damages on the robot.

208 The hammer was released at various timings of the
 209 gait so that the perturbation could be applied at vari-
 210 ous gait phases that covered a whole single gait cycle.
 211 Time instants of the hammer impact were set within the
 212 interval between 7,600 and 10,300 ms from the begin-
 213 ning of the gait. Those impact timings were separated
 214 by 100 ms, and hence, responses of the robot against 28
 215 different impact timings covering the single gait cycle
 216 were examined. The magnitude of every perturbation
 217 was almost the same, and the peak impact force mea-
 218 sured by a digital force gage sensor (FGX-50, Nihon-
 219 Densan Sympo, Kyoto) was about 4 N regardless of the
 220 horizontal position of the impact. The kinetic energy
 221 of the hammer and, of course velocity in the horizon-
 222 tal direction were maximal when the pendulum was at
 223 its lowest point, and their values were approximately
 224 0.2 Nm and 1.3 m/s, respectively. In terms of the kinetic
 225 energy, the small differences in the magnitude of the
 226 perturbation due to the change of position of the robot
 227 at the impact varied to less than $\pm 15\%$ of the maximum
 228 value. The hammer contact point on the robot's back
 229 changed from side to side, since the body trunk swung
 230 from side to side with its amplitude about 4 cm with the
 231 gait period. Because of this, the hammer contact point

on the robot's back was slightly left side of the trunk for the first half cycle and right side for the latter half cycle. Moreover, the control gait of the robot always tended to curve slightly leftward due to uncontrollable characteristics of the robot. For these reasons, the impacts during the first and the latter halves of the cycle were not necessarily exactly the same. However, these differences were small with respect to the most important factor: the instants of the hammer's impact with the robot with respect to the gait cycle.

Within the examined impact time interval between 7,600 and 10,300 ms, the gait phase of the robot with the control motion data was as follows. The left foot took off the ground at the time about 7,750 ms, the start of the left swing phase. The time interval from 7,750 to 9,050 ms was the first half cycle of the gait. The early part of this interval until 8,400 s was the right single-stance phase, which could be further divided into the early and late swing of the left leg, and the remaining interval was the double-stance phase. The subsequent time interval from 9,050 to 10,300 ms was the latter half cycle of the gait which started with the left single-stance phase or the early swing phase of the right leg, and then the late swing of the right leg, followed by the double-stance phase.

2.4 Responses of robot to the impact

The impacts made by the hammer acted as the perturbations to the humanoid gait. In response to each impact applied at various phases of the gait, we modified the movement of the robot. An appropriate modification of the robot movement, which we should clarify in this study, might depend on the given perturbation phase. The modification of the robot movement examined here included two parameters. The most important parameter was the amount of phase reset Δn in the unit of milliseconds. That is, in response to the impact, the control motion data was phase shifted. Let us denote the control motion data as $\{x_n\}$ where the subscript n runs from 1 to $N = 17,900$. The phase shift here means that the motion data after the impact was switched from the control motion data $\{x_n\}$ to the *modified motion data* or, equivalently, *phase-shifted motion data* $\{x_{n-\Delta n}\}$. It was phase advanced by an amount of Δn ms, or $(\Delta n/2, 600) \times 100\%$ short compared to the control gait cycle, when $\Delta n < 0$ in one case. It was phase delayed, i.e., $(\Delta n/2, 600) \times 100\%$ long, when $\Delta n > 0$ in another case. When $\Delta n = 0$, the motion data was not modified, i.e., the same as the control motion data.

The second parameter was the transient duration $\tau > 0$ in the unit of milliseconds. When the motion data was phase shifted from $\{x_n\}$ to $\{x_{n-\Delta n}\}$ at time m ms in response to the perturbation, the desired joint angles

at times m and $m + 1$ could change largely for large $|\Delta n|$, leading to a very large joint angular velocity of the robot. Although such a large joint angular velocity required a large amount of motor torque, which could be harmful to the system, our robot system could manage to achieve the corresponding quick movement. In our experiments, however, such a situation was avoided by introducing the transient duration started at the impact and ended at τ ms after the impact. We introduced the transient duration because it could be an influential factor that determines whether or not the perturbed gait could avoid a falling during human and simulated human gait as shown in the previous works (Yamasaki et al. 2003a,b). In order to realize the transient duration, for the impact at time m , we set the modified motion data at time m as x_m , and at time $m + \tau$ as $x_{m-\Delta n+\tau}$. The modified motion data from the time m to $m + \tau$ was determined so that every component of x_m and $x_{m-\Delta n+\tau}$ was connected smoothly using third-order spline functions. Figure 2 illustrates this situation, in which a case with $\Delta n = -800$ ms (the phase was advanced about 30% of the control gait cycle) in response to the impact at 9,500 ms is exemplified. In the figure, hip, knee and ankle joint angles of right leg for the control motion data (dotted curves) and the modified, phase-shifted motion data (solid curves) are superposed. For the first several hundred milliseconds before the impact, waveforms of the control and modified motion were identical. At the impact (the left-most vertical line), they started to separate. In this case, we set the transient duration τ as 200 ms, which corresponds to the interval from the left-most to the second vertical line. Comparing the solid and dotted curves after $\tau = 200$ ms from the impact, it can be seen that the waveforms were the same but the solid modified motion data was phase advanced. See Yamasaki et al. (2003a) for a similar method and a detailed procedure.

In this paper, $\tau = 200$ ms, which corresponded to about 8% of the control gait cycle, was used mostly, except in only two cases where $\tau = 600$ ms corresponding to a long transient was also examined in addition to $\tau = 200$ ms for which the robot was fallen by the impact; but it was highly expected that a longer transient might improve the response of the robot to avoid the fall. Influence of the transient duration on the perturbed robot gait was not be extensively examined in this study, but it has been demonstrated that the transient duration, in addition to the amount of phase reset, was a crucial and phase-dependent determinant of the gait stability against the perturbation during human and simulated human gaits (Yamasaki et al. 2003a,b). See Sect. 4 for related arguments on the transient duration.

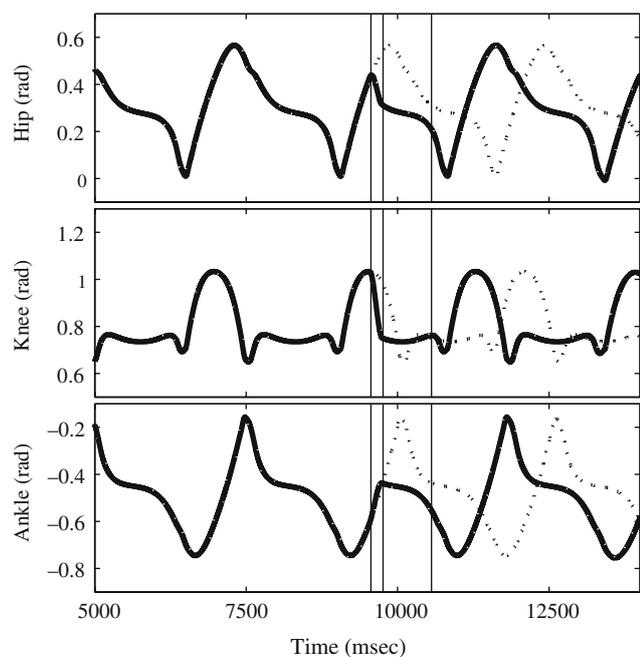


Fig. 2 Procedure of phase resetting in which the motion data was switched from the control to a phase-shifted motion data in response to a detection of the hammer impact. Hip, knee and ankle joint angles of right leg for the control (*dotted curves*) and the phase-shifted motion data (*solid curves*) are superposed. For the first several hundred milliseconds before the impact, waveforms of the control and the phase-shifted motion were the same. At the impact (*left-most vertical line*), they started separation. In this case, the transient duration τ was 200 ms, corresponding to the interval from the *left-most* to the *second vertical line*. Comparing the *solid* and *dotted curves* after $\tau = 200$ ms from the impact, the waveforms are the same but the *solid curves* are phase advanced ($\Delta n = -800$ ms). The time interval from the *second* to the *third vertical line* was 800 ms. See text for details

output crossed a threshold (14.6 m/s^2). For safety of the experiment, when the robot started falling largely, the local servo mechanism was switched off before the robot completely fell down the ground. This was judged by the output value of the angular velocity sensor (ω_z) with respect to the vertical z axis. More precisely, if an event either $\omega_z < -1.25$ or $\omega_z > 1.13 \text{ rad/s}$ was detected, the local servo was switched off 1,000 ms after the detection, so that the robot stopped the gait motion by letting all joints move freely.

Optimal amounts of phase reset that could avoid falling against the perturbation were systematically explored for various perturbation phases. To complete this, we made 588 impact experiments consisting of different timings of the hammer impact and different amounts of phase reset in response to the impact. For a fixed given amount of the phase reset, the robot performed walking 28 times. For each walking, a perturbation with different impact timing, ranging from 7,600 to 10,300 ms with 100 ms steps, was applied. Such 28 experiments were carried out for 21 different amounts of the phase reset, ranging from $-1,000$ to $1,000$ ms (corresponding to the phase advance and phase delay about 38% of the control gait cycle) including zero phase reset. By those, we obtained 588 pairs of the experimental conditions on the perturbation phase and the amount of the phase reset. When the robot could keep walking despite the perturbation for a given timing and an amount of the reset, the corresponding condition set was considered as “success,” otherwise “fail” in which the robot fell down for that timing and reset condition. Note that we determined the intensity of the perturbation (i.e., the initial height of the hammer) so that, even when $\Delta n = 0$ (with no phase reset), the robot did not fall for some intervals of the perturbation phase, which was roughly overlapped with the timing of double support phase of the robot. If the perturbation intensity was higher and the robot could not keep walking without phase reset for any impact timing, the current phase reset mechanism could not work out.

3 Results

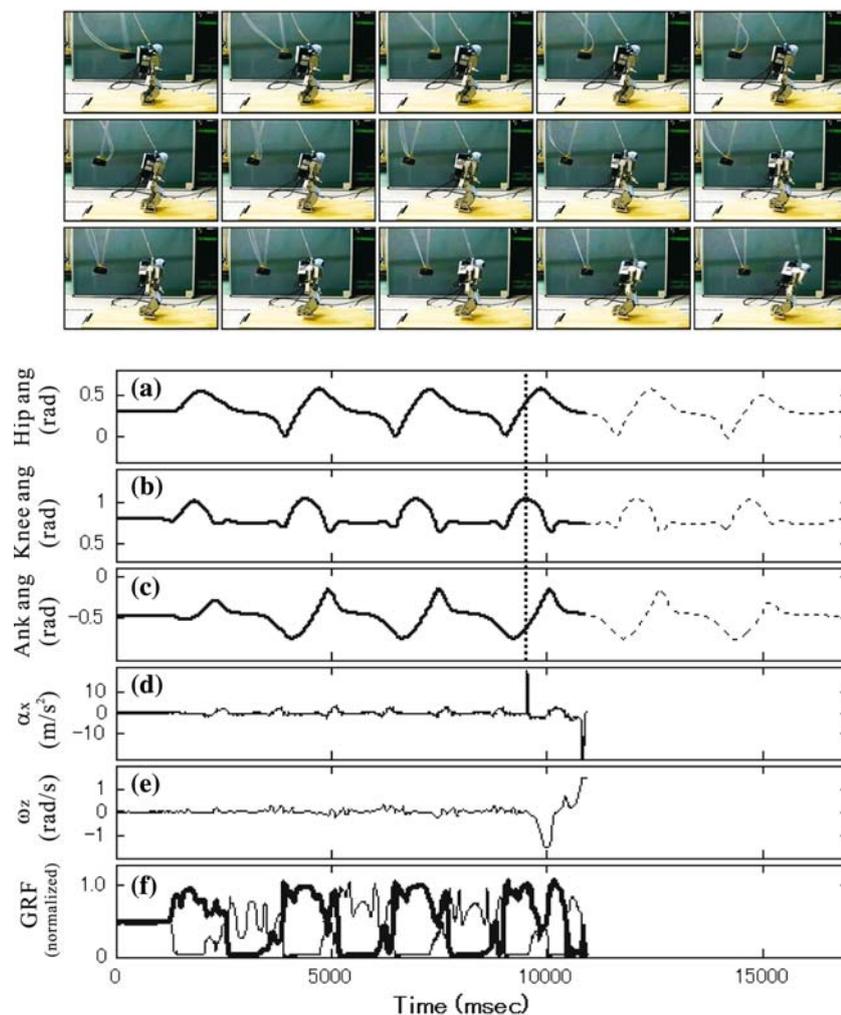
Figure 3 exemplifies a response of the robot to the hammer perturbation with the impact at 9,500 ms after the gait onset, which corresponded to the late swing phase of the right leg, when no phase reset was made. All of the joints changed strictly in accordance with the control motion data even after the detection of the hammer impact. In this case, the robot fell down the ground in a second. Note that before the robot fell completely down to the ground, the local servo mechanism

An appropriate set of the two parameter values, namely, Δn and τ , may provide a way of response for the robot to a given timing of the perturbation so that the robot can continue walking against the hammer impact. If the values of these two parameters are not appropriate, the robot may be fallen by the impact. In this study, we changed these two parameter values, in particular, the value of Δn in a wide range, for each of various timings of the perturbation to look for the optimal values of these parameters.

The impact on the back of the robot was detected by the three-axial acceleration sensor in the body. In particular, we used the acceleration in the front-back direction (α_x). The output value of this sensor varied oscillatorily but with small amplitude during the control gait. When the hammer impacted on the back of the robot, the output value of this sensor markedly and rapidly increased to form a delta function like waveform. The impact time was defined when the sensor

Fig. 3 Response of the humanoid to the impact at $t = 9,500$ ms (the late swing of the right leg) in case without phase reset, leading to a fall.

Top A sequence of picture frames with 100 ms steps (time evolves from *top-left* just around the impact to *bottom-right*). *Panels a–c* Hip, knee and ankle joint angles of right leg. *Solid curves* are actual robot motions, and *dotted curves* are the control motion data. *d, e* The body acceleration in the front–back direction and yaw angular velocity of the body. *f* Ground reaction forces (GRF) of the left (*thick curve*) and the right (*thin curve*) feet. GRF was normalized by the total weight of the robot. The *dotted vertical line* common to *a–c* indicates the instance of the impact detection corresponding to the delta function like change in the body acceleration shown in the *panel d*

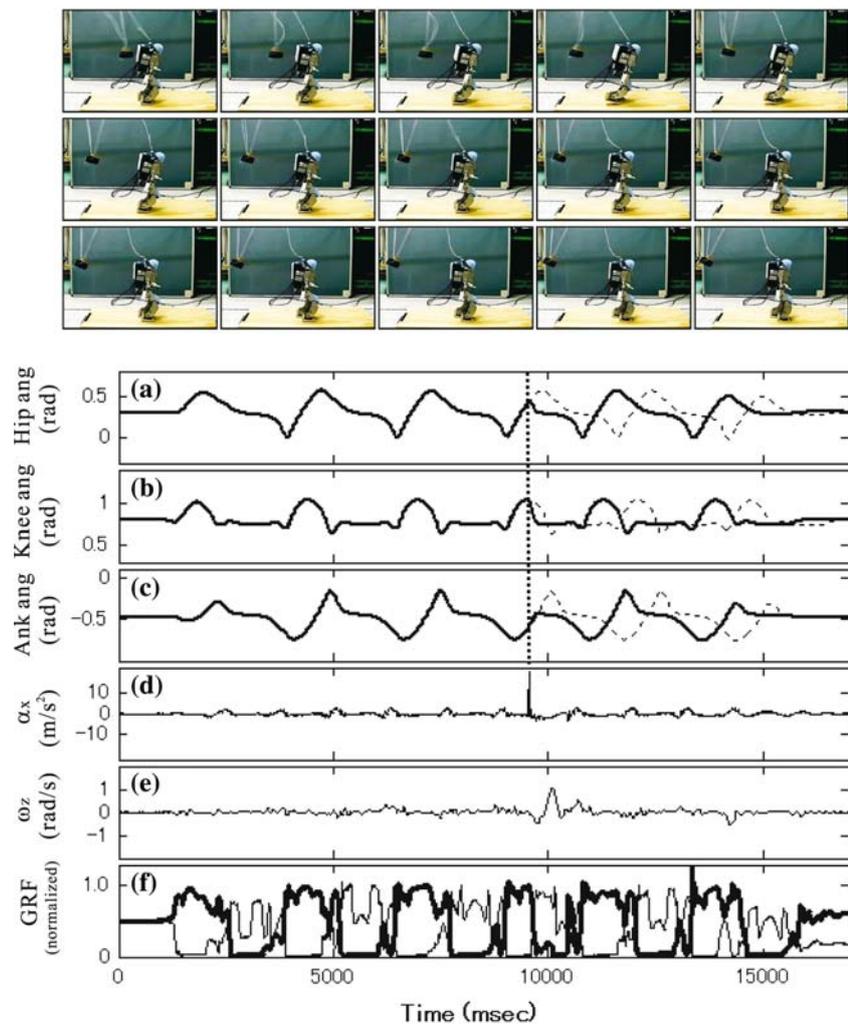


of all joints were switched off for safety as mentioned in the method. (See Electronic Supplementary Material Movie 1.)

For the same perturbation with the impact at 9,500 ms at the late swing of the right leg, the phase reset of $\Delta n = -800$ ms (phase advanced about 30% of the control gait cycle) of the motion data in response to the impact detection with the transient duration $\tau = 200$ ms could lead to the maintenance of the gait (Fig. 4). That is, when the control motion data was switched to the corresponding phase-shifted motion data in response to the detection of perturbation, the robot could continue walking without falling after the perturbation. (See Electronic Supplementary Material Movie 2.) In this case, the right leg which was in the late swing at the impact touched the ground quickly after the impact. This response was similar to the lowering strategy that has been identified during human stumbling reaction when the obstacle or the force perturbation at the lower leg from behind was applied at late swing phase (Schillings et al. 2000; Forner Cordero et al. 2003, 2004).

Another example was for the perturbation with the impact at 9,600 ms after the gait onset (late right swing) as shown in Fig. 5. The robot fell down without phase reset for the perturbation with this timing, but the walking could be maintained when the phase reset by amount of 600 ms (phase delay about 20% of the control gait cycle) was employed. (See Electronic Supplementary Material Movies 3 and 4.) In this case, the right leg, which was also in the late swing at the impact, was elevating quickly after the impact, and the swing phase was performed again. The corresponding motion of the robot was similar to the one observed in the human elevating strategy that has been identified during stumbling reaction. Note, however, that the elevating strategy during human gait has been observed when the obstacle perturbation was applied at early swing phase (Schillings et al. 2000; Forner Cordero et al. 2003, 2004), whereas the phase-delayed response with the elevating-like motion shown here was for the perturbation at the late swing phase. See Sect. 4 for this discrepancy. Despite of this discrepancy, the motions of the robot during

Fig. 4 Response of the humanoid to the impact at $t = 9,500$ ms as in Fig. 3, but with the phase resetting by the amount of -800 ms (phase advanced about 30% of the control gait cycle, transient duration $\tau = 200$) that helps avoiding the fall. See Fig. 3 caption. In *a-c*, the *solid curves* are phase advanced compared to the *dotted control motion data* after the perturbation



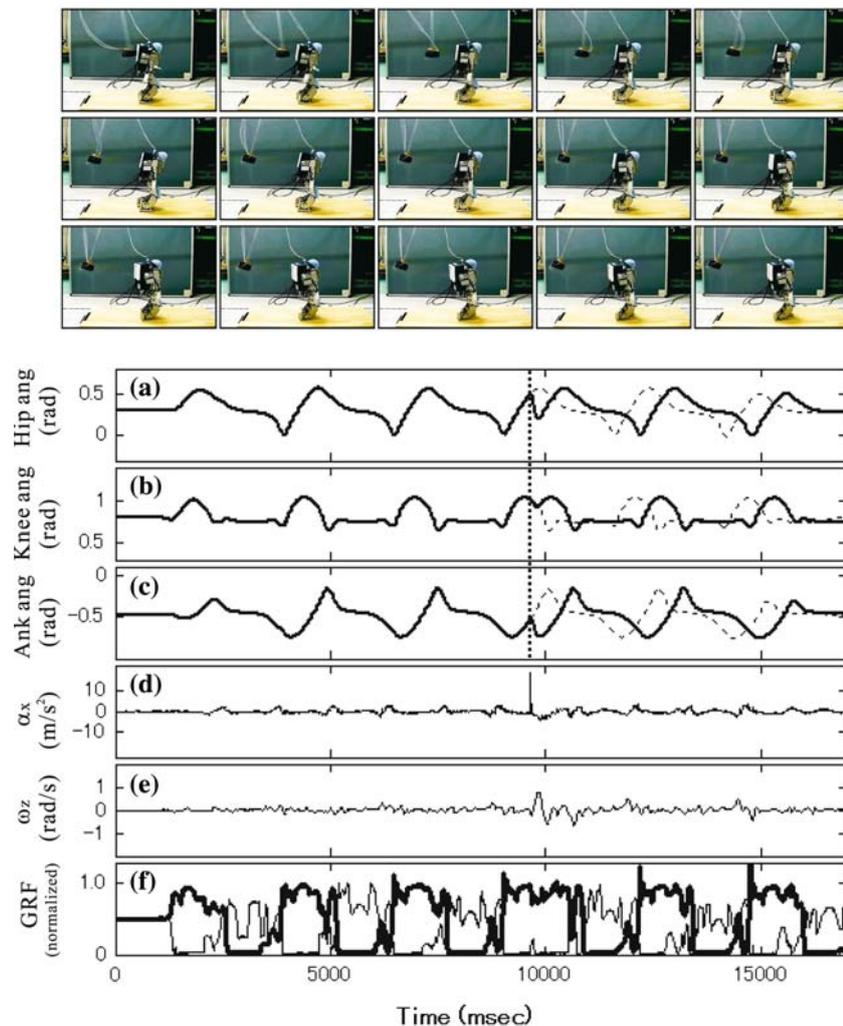
447 the phase-advanced responses (Fig. 4) and the phase-
 448 delayed responses (Fig. 5), respectively, mimicked well
 449 the human stumbling reactions with the lowering and
 450 elevating strategies.

451 Figure 6 summarized results of our systematic exploration
 452 of optimal amounts of phase reset for various
 453 perturbation phases. The horizontal axis common to the
 454 upper and lower panels is the time from the beginning of
 455 the gait, representing the impact time, or the gait phase
 456 in terms of percentage of one gait cycle, whose origin
 457 was set as the beginning of the single-stance phase of
 458 the right leg at 7,750 ms, at the impact. The vertical axis
 459 is the amount of phase reset examined. When the robot
 460 could keep walking despite the perturbation for a given
 461 timing and an amount of the reset, the corresponding set
 462 of the parameters (grid) for the success gait was marked
 463 with a square. Otherwise, no square marks were made,
 464 for which the robot fell down for that timing and reset
 465 (failed gait). The failed gait shown in Fig. 3 corresponds
 466 to the open circle located on the horizontal central line
 467 of the upper panel of Fig. 6. Together with Fig. 6 lower

468 panel, it could be confirmed that the impact timing at
 469 9,500 ms was the middle of single-stance phase in which
 470 the left foot was in contact with the ground and the
 471 right leg was in its swing phase. The phase-advanced
 472 gait shown in Fig. 4 corresponds to the filled square with
 473 open circle located at the grid (9,500, -800). The filled
 474 square with open circle at the grid (9,600, 600) corre-
 475 sponds to the gait with the phase delay reset shown
 476 in Fig. 5. One could imagine the functional shape of the
 477 optimal phase resetting curve from Fig. 6. That is, a phase
 478 resetting curve lying within the squared region, provides
 479 an optimal response of the robot to every timing of the
 480 impact.

481 In Fig. 6, one could also see that, for the impact at
 482 9,500 ms (right late swing) for example, relatively large
 483 amounts of phase advance (from -600 to $-1,000$ ms, cor-
 484 responding to 23–38% of the control gait cycle) could
 485 lead to the maintenance of gait against the impact. For
 486 this impact timing, intermediate amounts of phase delay
 487 (from 200 to 700 ms, corresponding to 8–27% of the con-
 488 trol cycle) could also lead to the maintenance of gait.

Fig. 5 Response of the humanoid to the impact at $t = 9,600$ ms (late right swing) with the phase resetting by the amount of 600 ms (phase delay about 20% of the control gait cycle, transient duration $\tau = 200$) that helps avoiding the fall. See captions of Figs. 3 and 4



489 That is, for the given impact timing, both the phase-
 490 advanced (lowering strategy like) and the phase-delayed
 491 (elevating strategy like) responses could avoid a falling.
 492 Figure 6 shows that, for the perturbations at the early
 493 swing, no or small phase reset was appropriate, and the
 494 optimal amounts of phase reset in both advanced and
 495 delayed directions increased as the gait phase at the
 496 impact increased in the right single-stance phase. See
 497 Sect. 4 for these results in comparison with the human
 498 gait.

499 The phase-delayed responses corresponding to the
 500 open squares at (8,500, 1,000) and (9,800, 1,000) at the
 501 beginning of the double stance in Fig. 6 examined with
 502 the transient duration $\tau = 600$ ms. For these cases, the
 503 control gait without phase reset could not avoid fall-
 504 ing despite that the impact was applied at the double-
 505 stance phase. Moreover the phase-delayed responses
 506 with $\Delta n = 1,000$ ms (38% phase delay) with $\tau = 200$ ms
 507 could not prevent the robot from falling. However, the
 508 phase-delayed reset with a longer transient duration

($\tau = 600$ ms) could avoid falling, showing that the tran-
 509 sient duration for the phase reset was also an important
 510 gait parameter determining a modification of gait tra-
 511 jectory when the perturbation was applied. The reason
 512 we examined these two cases with the long transient
 513 duration was as follows: these two grids, in particu-
 514 lar the condition (9,800, 1,000), were located close to
 515 the filled-square region for which the phase reset with
 516 200 ms transient led to the success gait. We expected a
 517 continuity of this region to larger amount of phase delay.
 518 However, it was not the case. That is, the motion of the
 519 robot with 1,000 ms phase shift and 200 ms transient was
 520 apparently too fast, and the right leg close to the ground
 521 contact phase fanned the air rapidly in the backward
 522 direction during the resetting motion (see Electronic
 523 Supplementary Material Movie 5), and it generated a
 524 large forward momentum, leading to destabilization of
 525 the posture. It was highly expected that the same amount
 526 of phase delay but with a long transient might not gen-
 527 erate a large forward momentum and could result in a
 528

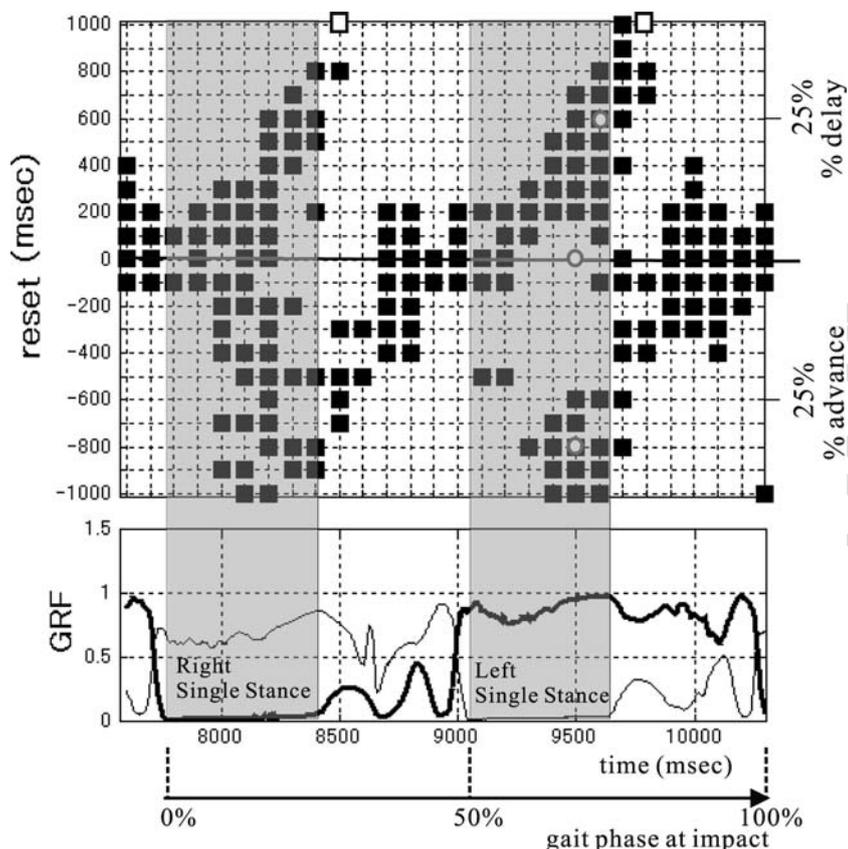


Fig. 6 *Top* Optimal amounts of the phase reset for various phases of the hammer impact. Horizontal axis common to the *upper* and *lower panels* is the time from the beginning of the gait, representing the impact time, or the gait phase in terms of percentage of one gait cycle, whose origin was set as the beginning of the single-stance phase of the right leg at 7,750 ms, at the impact. The vertical axis is the amount of phase reset examined. When the robot could keep walking despite the perturbation for a given timing and an amount of the reset, the corresponding set of the parameters (grid) for the success gait was marked with a *square*. Otherwise, no square marks were made, for which the robot fell

down for that timing and reset (failed gait). *Bottom* Averaged GRF acting on the left (*thick curve*) and the right (*thin curve*) foot. GRF was normalized by the total weight of the robot. The failed gait shown in Fig. 3 corresponds to the *open circle* located on the *horizontal central line* of the *upper panel*. The phase-advanced gait shown in Fig. 4 corresponds to the *filled square with open circle* located at the grid (9,500, -800). The *filled square with open circle* at the grid (9,600, 600) corresponds to the gait shown in Fig. 5. The phase-delayed responses corresponding to the *open squares* at (8,500, 1,000) and (9,800, 1000) were examined with the transient duration $\tau = 600$ ms. See text

529 reasonable retouch down of the right leg after the reset,
 530 leading to a success of the stumbling gait. This expecta-
 531 tion was right as summarized in Fig. 6. (See Electronic
 532 Supplementary Material Movie 6 for the corresponding
 533 gait.)

534 One could observe in Fig. 6 that the configuration of
 535 the squares for the first half of the cycle and that for
 536 the latter half cycle was similar but not the same. If the
 537 robot gait on our walk way were precisely straight and
 538 periodic, these two half cycles would have been symmet-
 539 rical. However, this was not the case in our experimen-
 540 tal setup. For this reason, for the early part of the latter
 541 half of the cycle (early right swing), the phase-advanced
 542 responses tended to be failed, although we could obtain

appropriate amounts of phase-advanced reset for the
 corresponding phase interval in the first half cycle (early
 left swing).

4 Discussion

We showed that there exist optimal amounts of phase
 reset that could prevent the walking humanoid robot
 from falling against a relatively large impulsive force
 perturbation in the anteroposterior direction applied
 at the robot's back. The obtained optimal amounts of
 phase reset depended on the gait phase (timing) of the

553 perturbation, by which we confirmed that the phase
554 resetting theory developed for the simple gait model
555 on the sagittal plane (Yamasaki et al. 2003a,b) could
556 be extended into the real-world gait as far as exam-
557 ined perturbations in the anteroposterior direction were
558 concerned.

559 The result shown in this paper could be interpreted
560 as follows. In the cases without phase reset, the pertur-
561 bation moved the system's state point on the limit cycle
562 outside the basin of attraction of the limit cycle, leading
563 to the fall of the robot. With an appropriate amount of
564 phase reset, a state point relocated by the perturbation
565 outside the basin of the limit cycle of the system without
566 phase reset becomes inside the basin of the limit cycle
567 of the system with phase reset, leading to the preven-
568 tion of the fall. Such an optimal amount of the phase
569 reset for every examined timing of the hammer impact
570 was identified by trying ten phase-advanced (from -100
571 to -1,000 ms, corresponding to the phase advance of
572 4-38% of the control gait cycle) and ten phase-delayed
573 (from 100 to 1,000 ms, corresponding to 4-38% of the
574 control cycle) modifications of the control motion data
575 in response to the detection of the hammer impact.

576 The result of this study was qualitatively consistent
577 with the ones reported for the perturbed human gait
578 (Kobayashi et al. 2000) and for the differential equation
579 model of human gait (Yamasaki et al. 2003a,b), imply-
580 ing that the phase reset mechanism during gait could
581 be a common and useful strategy for increasing gait
582 stability. It has been discussed that, for human motor
583 control, such a reflex-like response for trajectory mod-
584 ification might be beneficial to maintain desired cyclic
585 movements with low joint stiffness under the influence
586 of feedback transmission delay (Yamasaki et al. 2003a),
587 although the response of the robot examined in this
588 study merely emulated the reflex-like movement using
589 the high-gain local feedback mechanism (i.e., with very
590 high joint stiffness) that could never be realized in the
591 living animals. In the human stumbling reaction, two
592 strategies have been clarified (Schillings et al. 1999;
593 Forner Cordero et al. 2003). Those include the elevat-
594 ing strategy occurred for the stumble perturbation at
595 early swing, and the lowering strategy at late swing.
596 The elevating and lowering strategies are, respectively,
597 consistent with the delayed and advanced phase reset
598 responses as shown in Yamasaki et al. (2003a,b). In the
599 current robot experiment, for most of the perturbation
600 phases for which the phase reset could avoid the fall-
601 ing, there was a tendency that both phase-advanced and
602 phase-delayed responses, if appropriate, could avoid the
603 falling, implying that there is a freedom for "the control-
604 ler" to choose one of these two resets. It is worthwhile to
605 associate this result with the fact that, when the pertur-

606 bation is applied at a certain range of the mid swing in
607 human stumbling reaction, both the elevating and lower-
608 ing strategies could occur (Schillings et al. 1999; Forner
609 Cordero et al. 2003). Based on this result, Schillings et
610 al. (2000) made the following discussion: "The same ini-
611 tial reaction of the two strategies possibly provides the
612 CNS sufficient time to integrate information obtained
613 by various sensory receptors and supraspinal sources to
614 make an appropriate decision about the final behavioral
615 strategy." Delayed lowering strategy at early swing, in
616 which first elevating-like response appears right after the
617 perturbation and then switches to the lowering strategy,
618 could also be related to this discussion. The result of the
619 robot experiment suggests the following scenario: for a
620 certain range of the perturbation phases, both the phase-
621 advanced and phase-delayed resets could avoid the fall
622 in the sense of the mechanical stability during human
623 gait, but the response might not be predetermined at
624 the onset of the perturbation. The CNS, as the phase
625 controller in a sense of the current study, can choose
626 one of them based on the various integrated sensory
627 information.

628 Let us discuss the transient duration used for the
629 phase reset. The transient duration, in which the phase
630 reset was progressively achieved, might be an influential
631 determinant whether or not the robot with the resetting
632 gait trajectory could avoid a falling. In the human gait
633 and the simulated human gait experiments (Yamasaki
634 et al. 2003a,b), in which the perturbation applied at the
635 lower right leg by an impulsive tug from the behind was
636 used, it was shown that the phase advance with rela-
637 tively long transient, 30% of the gait cycle (~300 ms),
638 was optimal for the late swing perturbation, and the
639 phase delay with short transient, 5-10% (~100 ms) for
640 the early swing perturbation. The transient duration
641 200 ms used in the current humanoid experiment was
642 about 8% of the gait cycle ($T \simeq 2,600$ ms), and it was in
643 the latter short transient range. Although only two cases
644 with the long transient (600 ms) responses were exam-
645 ined in this paper, they exemplified that perturbed gaits
646 with a selected amount of phase reset could be differ-
647 ent (success or fail) depending on the transient duration.
648 One important factor that caused the difference could be
649 the inertia force (momentum) generated by the motion
650 during the phase reset. That is, a large amount of phase
651 reset with a short transient duration results in a rapid
652 movement and thus generating a large inertia force, but
653 that with a long transient does not. Effect of such an
654 inertia force on the gait stability against the perturba-
655 tion is phase dependent. That is, the inertia force caused
656 by the motion during the reset could counterbalance or
657 foment the momentum generated by the perturbation.
658 The effect of this inertia force on the gait stability must

659 be evaluated together with the momentum generated by
660 the ground reaction force acting on the body during or
661 after the phase reset. For the two cases described in this
662 paper, it was visually apparent that the large inertia force
663 generated during the phase delay response fomented the
664 forward momentum, leading to the gait destabilization.
665 We thus tried a long transient duration to reduce the
666 amount of inertia force, and obtained two cases exem-
667 plifying a role played by the transient duration of the
668 phase reset. For the sake of completeness in the current
669 study, we should have varied systematically the transient
670 duration as in the simulated gait. However, the human-
671 oid experiment with the hammer impacts over hundreds
672 of times was too tough to achieve for the machine. The
673 systematic modification of the transient durations and
674 analyses based on mechanical dynamics could be topics
675 for future research.

676 [Forner Cordero et al. \(2004\)](#) discussed relations
677 between physical constraints on possible hip torques
678 compensating the forward trunk motion and swing speed
679 during human gait responses in the first double-stance
680 phase just after the perturbation simulating a stumble.
681 They claimed that the lowering (and delayed lower-
682 ing) strategy for the late swing perturbation resulted
683 in shorter step lengths and had lower hip torques due
684 to the physical constraints, implying a difficulty in com-
685 pensating the forward trunk motion in the first double-
686 stance phase. Thus, one more or several compensation
687 steps are needed. This is consistent with the long tran-
688 sient duration for the phase-advance responses shown
689 in [Yamasaki et al. \(2003a,b\)](#), in which early part of the
690 second step of contralateral swing leg after the quick
691 touch down of the perturbed foot is still in the phase
692 resetting transient, and it is accompanied by a quick
693 motion. In the current humanoid experiment, the phase-
694 advance responses with the short transient for the late
695 swing perturbation could avoid the falling. One reason
696 for this discrepancy could be a relatively long period of
697 the humanoid gait (~2,600 ms) and slow walking veloc-
698 ity. That is, forward momentum in the control and the
699 perturbed gait was small. Hence, the lowering strategy
700 with the phase-advance response and thus short step in
701 our robot experiment did not necessarily encounter the
702 difficulty in compensating the forward trunk motion in
703 the first double-stance phase. In this sense, it is expected
704 that shorter transient duration for the lowering strategy
705 might be enough for slower gait speeds, and a human
706 gait experiment will be able to confirm this expectation.

707 Regarding quantitative aspects of the optimal phase
708 reset, the optimal amount of phase reset in the current
709 study for the robot was different from the ones obtained
710 for the human and simulated gaits. This difference might
711 be due to differences in the way of perturbation, in

712 the mechanical and physical characteristics (mass, iner-
713 tia, etc.) between the human and the robot, as well as
714 in the way of determination of the transient duration.
715 The latter two factors largely affect the trajectory of
716 the zero moment point (ZMP) during gait as discussed
717 below.

718 Zero moment point is defined as “a theoretical point”
719 such that the momentum caused by the external force
720 (the ground reaction force for gait) applied to ZMP
721 balances with other forces (the inertia and centrifugal
722 forces) that will be generated if the robot performs a
723 prescribed motion. The ZMP stability criterion ([Vuko-
724 bratovic et al. 1990](#)) has been used to prescribe an unper-
725 turbed gait trajectory and to modify the gait trajectory
726 in response to a perturbation in order to generate a
727 desired compensating gait trajectory. It examines, prior
728 to the gait execution, if ZMP trajectory for the pre-
729 scribed gait trajectory is always inside the foot support
730 area and the prescribed trajectory can be a solution of
731 the equation of motion of the robot. The modification
732 of the gait trajectory is carried out in response to the
733 perturbation. To this end, after the perturbation, the
734 foot contact times and their placements and the modi-
735 fied desired ZMP trajectory for the transient duration
736 are determined, and then the modified joint trajectory
737 is determined so that the ZMP of this gait coincides
738 with the modified desired ZMP. Note that there exist
739 infinitely many joint trajectories that are accompanied
740 with the single ZMP trajectory, implying that the deter-
741 minant of a specific joint trajectory is an ill-posed prob-
742 lem. Note also that, computationally, the equations of
743 motion of the robot are usually utilized to solve the
744 ill-posed problem. In this way, the determinations of the
745 modified desired ZMP trajectory and the corresponding
746 joint trajectory can specify the modified gait trajectory.
747 When one employs a strategy to compensate the pertur-
748 bation using an appropriate modification of the trunk
749 movement (hip joint trajectory) and/or modification of
750 the total ground reaction force vector without modify-
751 ing the foot contact times (but maybe with modifying its
752 location), the resultant trajectory may be able to avoid a
753 falling, but in this case the gait does not show the phase
754 reset. When a strategy that modifies the step length in
755 time (and maybe also in spatial location) to compensate
756 the perturbation is employed with or without consid-
757 ering ZMP criterion, the resultant gait may always be
758 accompanied with the phase reset. It is an open problem,
759 for human gait, whether the phase reset is just a conse-
760 quence of the modification of the foot contact times and
761 placements that are determined based on the ZMP crite-
762 rion or the phase reset causes the modification of the foot
763 contact times and placements during human perturbed
764 gait, or even both of them are concerned. See the work

765 by Honda (Hirai et al. 1998) for an integrated example
766 of a humanoid gait control, in which the role played by
767 the foot landing position control (landing timing control
768 seems to be made implicitly) is considered to be rather
769 limited for stabilizing the gait.

770 If the CNS concerns the ZMP to determine the mod-
771 ified gait trajectory, regardless of the use of phase reset,
772 the CNS should concern the equations of motion, imply-
773 ing the necessity of an internal model of the body dynam-
774 ics in the CNS. In this study, the optimal amount of phase
775 resets were determined by examining various values as
776 many as possible without using the ZMP stability crite-
777 rion. This may correspond to, for the CNS, to con-
778 struct a look-up table relating the perturbation timing
779 and the optimal amount of the phase reset. This is pos-
780 sible when a way to apply a perturbation (such as the
781 hammer impact intensity, direction, the impact location
782 of the robot's body, etc, in this study) is fixed. Since
783 the human gait is robust and adaptive against various
784 types of perturbations, it is not possible to consider a
785 look-up table as a feasible physiological mechanism to
786 trigger a stumbling reaction in humans. Thus, usage of
787 the internal model of the body dynamics to determine
788 the modified gait trajectory is expected.

789 Other lines of research have shown that biped robot
790 stability can be achieved without the application of the
791 ZMP stability criterion (e.g., McGeer 1990; Collins et al.
792 2005; Van der Linde 1999), where natural dynamics of
793 inverted-pendulum-like body of the biped robot without
794 active joint torques or with less amount of active torques
795 can realize stable biped gaits along a down slope or on
796 a level ground. The stability of such passive gaits does
797 not explicitly address prescription of desired gait trajec-
798 tory and modification of it in response to perturbations,
799 but physical parameters of the body links and appropri-
800 ate viscoelasticity of joints determine the gait trajectory
801 "dynamically" as a limit cycle. Although the trajectory
802 modification in response to perturbations is achieved
803 only passively during such passive gaits, the state point
804 of the robot asymptotes to the limit cycle if it is inside
805 the basin of the limit cycle with some amount of phase
806 reset. The responses shown in this study were similar
807 to this, but the modification of the gait trajectory per-
808 formed in this study was not passive, and the gait phase
809 was actively reset so that the state point after the per-
810 turbation became inside the limit cycle. Revealing neu-
811 ral mechanisms that are responsible for the active reset
812 could be an important issue for future research. Possi-
813 ble candidates for the mechanisms are, for example, the
814 involvement of the internal model of gait dynamics as
815 mentioned above, and active reflex control of the muscle
816 impedance among others.

817 Several previous studies have implemented phase
818 resetting mechanisms to biped robots in order to
819 increase gait stability (e.g., Tsuchiya et al. 2003;
820 Nakanishi et al. 2004). Tsuchiya et al. (2003) proposed
821 a biped gait control scheme using coupled phase oscil-
822 lators, and introduced feedback pathway directly from
823 a foot sensor to the corresponding oscillator to reset its
824 oscillation phase. In the study by Nakanishi et al. (2004),
825 interconnections among oscillators, as well as feedback
826 gains to the coupled oscillators inducing the phase reset-
827 ting, were determined through learning processes. Both
828 cases show that the phase resetting mechanism contrib-
829 utes to increasing gait stability against environmental
830 perturbations. It is worthwhile to emphasize that inten-
831 sities of the examined perturbations in those studies,
832 and thus the amounts of phase reset induced, were rela-
833 tively small compared to the ones concerned in the
834 present study. It is likely that realizing phase-dependent
835 resetting with a large amount using nonlinear oscilla-
836 tors might not be easy, since the amount of phase reset
837 is determined by both intrinsic dynamics of the oscil-
838 lator and characteristics of feedback signals. Moreover,
839 in those studies, only foot contact events were used to
840 trigger phase resetting of the oscillators, whereas it is
841 not the case for the present study and in human gait
842 response to the perturbation examined in Kobayashi
843 et al. (2000). Corrective modulation of the gait trajec-
844 tory including the resetting triggered by the foot con-
845 tact seems to work well for phase-advanced case, which
846 would be usual if a swing foot is forced to make an early
847 contact. When phase-delayed responses corresponding
848 to the stumbling with elevating strategy are optimal to
849 avoid falling, a resetting triggered at the first foot con-
850 tact after the perturbation might be too late, and a reset-
851 ting immediately after the perturbation, before the foot
852 contact, is required.

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